

Conjunction			Disjunction			Implication		
p	q	$p \wedge q$	p	q	$p \vee q$	p	q	$p \Rightarrow q$
V	V	V	V	V	V	V	V	V
V	F	F	V	F	V	V	F	F
F	V	F	F	V	V	F	V	V
F	F	F	F	F	F	F	F	V

Law of noncontradiction

$$p \wedge \neg p \Leftrightarrow F$$

Law of the excluded middle

$$p \vee \neg p \Leftrightarrow V$$

Double Negation

$$\neg(\neg p) \Leftrightarrow p$$

Commutativity

Conjunction

$$p \wedge q \Leftrightarrow q \wedge p$$

Disjunction

$$p \vee q \Leftrightarrow q \vee p$$

Associativity

Conjunction

$$(p \wedge q) \wedge r \Leftrightarrow p \wedge (q \wedge r)$$

Disjunction

$$(p \vee q) \vee r \Leftrightarrow p \vee (q \vee r)$$

Neutral Element

Conjunction

$$p \wedge V \Leftrightarrow p$$

Disjunction

$$p \vee F \Leftrightarrow p$$

Absorbing Element

Conjunction

$$p \wedge F \Leftrightarrow F$$

Disjunction

$$p \vee V \Leftrightarrow V$$

Idempotence

Conjunction

$$p \wedge p \Leftrightarrow p$$

Disjunction

$$p \vee p \Leftrightarrow p$$

Distributive Property

Conjunction over Disjunction

$$p \wedge (q \vee r) \Leftrightarrow (p \wedge q) \vee (p \wedge r)$$

Disjunction over Conjunction

$$p \vee (q \wedge r) \Leftrightarrow (p \vee q) \wedge (p \vee r)$$

Properties of Implication

Transitive

$$(p \Rightarrow q) \wedge (q \Rightarrow r) \Rightarrow (p \Rightarrow r)$$

Implication and Disjunction

$$(p \Rightarrow q) \Leftrightarrow \neg p \vee q$$

Negation

$$\neg(p \Rightarrow q) \Leftrightarrow p \wedge \neg q$$

Contrapositive of an Implication

$$(p \Rightarrow q) \Leftrightarrow (\neg q \Rightarrow \neg p)$$

Properties of Equivalence

Transitive

$$[(p \Leftrightarrow q) \wedge (q \Leftrightarrow r)] \Rightarrow (p \Leftrightarrow r)$$

Negation

$$\neg(p \Leftrightarrow q) \Leftrightarrow [(p \wedge \neg q) \vee (q \wedge \neg p)]$$

De Morgan's laws

Negation of a Conjunction

$$\neg(p \wedge q) \Leftrightarrow \neg p \vee \neg q$$

Negation of a Disjunction

$$\neg(p \vee q) \Leftrightarrow \neg p \wedge \neg q$$

De Morgan's laws

Negation of Universal Quantifier

$$\neg(\forall x, p(x)) \Leftrightarrow \exists x: \neg p(x)$$

Negation of Existential Quantifier

$$\neg(\exists x: p(x)) \Leftrightarrow \forall x, \neg p(x)$$