

Euler's Polyhedral Formula

$$F + V = E + 2$$

 $F$ : Face $V$ : Vertex $E$ : Edge

Sum of interior angles of a regular polygon

$$S_i = (n - 2) \times 180^\circ$$

 $n$ : Number of sides

Pythagorean theorem

$$H^2 = C_1^2 + C_2^2$$

Hypotenuse:  $H$ Leg:  $C_1$  e  $C_2$ 

Distance between two points

$$\overline{AB} = \sqrt{(x_1 - x_2)^2 + (y_1 - y_2)^2}$$

$$\begin{aligned} & \text{ex: } A(8, 2) \text{ e } B(4, -1) \\ & \overline{AB} = \sqrt{(8 - 4)^2 + (2 + 1)^2} \Leftrightarrow \\ & \overline{AB} = \sqrt{16 + 9} \Leftrightarrow \overline{AB} = 5 \end{aligned}$$

Midpoints

$$M\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$$

$$\begin{aligned} & \text{ex: } A(2, 6) \text{ e } B(4, -2) \\ & M\left(\frac{2+4}{2}, \frac{6-2}{2}\right) \Leftrightarrow M(3, 2) \end{aligned}$$

Slope–intercept form

Slope:  $m$ , Y intercept:  $b$ 

$$y = mx + b$$

Vector Form

Direction vector:  $\vec{u}(u_1, u_2, u_3)$ Point  $(x_0, y_0, z_0)$ 

$$(x, y, z) = (x_0, y_0, z_0) + k(u_1, u_2, u_3), k \in \mathbb{R}$$

Equation of a straight line

Cartesian Form

Direction vector:  $\vec{u}(u_1, u_2, u_3)$ Point  $(x_0, y_0, z_0)$ 

$$\frac{x - x_0}{u_1} = \frac{y - y_0}{u_2} = \frac{z - z_0}{u_3}$$

Parametric Form

Direction vector:  $\vec{u}(u_1, u_2, u_3)$ Point  $(x_0, y_0, z_0)$ 

$$\begin{cases} x = x_0 + Ku_1 \\ y = y_0 + Ku_2, k \in \mathbb{R} \\ z = z_0 + Ku_3 \end{cases}$$

Cartesian Form

Normal vector:  $\vec{u}(n_1, n_2, n_3)$ Point  $(x_0, y_0, z_0)$ 

$$n_1(x - x_0) + n_2(y - y_0) + n_3(z - z_0) = 0$$

Equation of a plane

Scalar Form

Normal vector:  $\vec{u}(n_1, n_2, n_3)$ 

$$n_1x + n_2y + n_3z + d = 0$$

Equation of a circle

Center  $(x_0, y_0)$  and radius  $r$ 

$$(x - x_0)^2 + (y - y_0)^2 = r^2$$

Equation of a Sphere

Center  $(x_0, y_0, z_0)$  and radius  $r$ 

$$(x - x_0)^2 + (y - y_0)^2 + (z - z_0)^2 = r^2$$

Equation of an Ellipse

Center  $(h, k)$  Axis  $a$  and  $b$ 

$$\left(\frac{x - h}{a}\right)^2 + \left(\frac{y - k}{b}\right)^2 = 1$$