

Average rate of change between two points

Slope of the Secant Line $[a, b]$

$$SSL = \frac{f(b) - f(a)}{b - a}$$

Rate of change at a point

$$f'(x_0) = \lim_{x \rightarrow x_0} \frac{f(x) - f(x_0)}{x - x_0} \quad f'(x_0) = \lim_{h \rightarrow 0} \frac{f(x_0 + h) - f(x_0)}{h}$$

Constant

$$a' = 0$$

ex: $4' = 0$

Multiplication by constant

$$(mx)' = m$$

ex: $(3x)' = 3$

Power Rule

$$(u^n)' = n \times u^{n-1} \times u'$$

ex: $((6x)^5)' = 5(6x)^4 \times (6x)' = 5(6x)^4 \times 6$

Root

$$(\sqrt[n]{u})' = \frac{u'}{n \times \sqrt[n]{u^{n-1}}}$$

ex: $(\sqrt{2x})' = \frac{(2x)'}{2 \times \sqrt{2x}} = \frac{1}{\sqrt{2x}}$

Exponential

$$(a^u)' = u' \times a^u \times \ln a$$

ex: $(7^{3x})' = 3 \times 7^{3x} \times \ln 7$

Exponential base e

$$(e^u)' = u' \times e^u$$

ex: $(e^{2x})' = 2 \times e^{2x}$

Sum Rule

$$(u + v)' = u' + v'$$

ex: $(2x + 5)' = (2x)' + 5' = 2$

Product Rule

$$(u \times v)' = u'v + uv'$$

ex: $(x^2 \times e^x)' = (x^2)'e^x + x^2(e^x)' = 2xe^x + x^2e^x$

Quotient Rule

$$\left(\frac{u}{v}\right)' = \frac{u'v - uv'}{v^2}$$

ex: $\left(\frac{x+1}{2x}\right)' = \frac{(x+1)' \times (2x) - (x+1) \times (2x)'}{(2x)^2}$

Chain Rule

$$(g \circ f)' = g'(f) \times f'$$

ex: $g(x) = 2x^2; g'(x) = 4x; f(x) = 2x; f'(x) = 2$
 $(g \circ f)' = 4(2x) \times 2$

Sine

$$(\sin u)' = u' \times \cos u$$

ex: $(\sin(6x))' = 6 \times \cos(6x)$

Cosine

$$(\cos u)' = -u' \times \sin u$$

ex: $(\cos(3x))' = -3 \times \sin(3x)$

Tangent

$$(\tan u)' = \frac{u'}{\cos^2 u}$$

ex: $(\tan(x))' = \frac{1}{\cos^2 x}$

Logarithms

$$(\log_a u)' = \frac{u'}{u \times \ln a}$$

ex: $(\log_4(6x))' = \frac{(6x)'}{6x \ln 4} = \frac{6}{6x \ln 4} = \frac{1}{x \ln 4}$

Natural logarithm

$$(\ln u)' = \frac{u'}{u}$$

ex: $(\ln(5x))' = \frac{(5x)'}{5x} = \frac{5}{5x} = \frac{1}{x}$