

Complex number $z = a + bi$

Conjugate $\bar{z} = a - bi$

Symmetry $-z = -a - bi$

Equality $a + bi = c + di \Leftrightarrow a = c \wedge b = d$

Addition $(a + bi) + (c + di) = (a + c) + (b + d)i$

Subtraction $(a + bi) - (c + di) = (a - c) + (b - d)i$

Multiplication $(a + bi) \times (c + di) = (ac - bd) + (ad + bc)i$

Algebraic Form Division $\frac{a + bi}{c + di} = \frac{a + bi}{c + di} \times \frac{c - di}{c - di} = \frac{ac + bd}{c^2 + d^2} + \frac{bc - ad}{c^2 + d^2}i$

Inverse $z^{-1} = \frac{1}{z}$ $z^{-1} = \frac{1}{|z|^2} \cdot \bar{z}$

$\bar{\bar{z}} = z$

$|z| = |\bar{z}|$

Properties $|z|^2 = z \cdot \bar{z}$

$Re(z) = \frac{z + \bar{z}}{2}$

$Im(z) = \frac{z - \bar{z}}{2i}$

Angle $arg(z) = \theta$ $\theta = \tan^{-1}\left(\frac{b}{a}\right)$

Exponential to Algebraic form conversion

Distance $|z|$ $|z| = \sqrt{a^2 + b^2}$

Complex number $z = |z| \cdot e^{i\theta}$ $z = |z| \cdot (\cos \theta + i \sin \theta)$

Conjugate $\bar{z} = |z| \cdot e^{i(-\theta)}$

Symmetry $-z = |z| \cdot e^{i(\theta+\pi)}$

Multiplication $z_1 \times z_2 = |z_1||z_2| \cdot e^{i(\theta_1+\theta_2)}$

Exponential form

$$\begin{aligned} z_1 &= |z_1| \cdot e^{i\theta_1} \\ z_2 &= |z_2| \cdot e^{i\theta_2} \end{aligned}$$

Division
$$\frac{z_1}{z_2} = \frac{|z_1|}{|z_2|} \cdot e^{i(\theta_1-\theta_2)}$$

Exponentiation $z^n = |z|^n \cdot e^{in\theta}$

Radicals $\sqrt[n]{|z| \cdot e^{i\theta}} = \sqrt[n]{|z|} \cdot e^{i\left(\frac{\theta+2k\pi}{n}\right)}, k \in \{0, \dots, n-1\}, n \in \mathbb{N}$